ON THE SUBGROUP GENERATED BY AUTOCOMMUTATORS

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It is well-known that the set of all commutators in a group is not necessarily a subgroup, see for instance the nice survey by L-C. Kappe and R.F. Morse [4]. Many authors have considered subsets of a group G related to commutators asking if they are subgroups.

Now let (G, +) be an abelian group. With $g \in G$ and $\varphi \in Aut(G)$, the automorphism group of G, we define the autocommutator of g and φ as

$$[g,\varphi] = -g + g^{\alpha}.$$

We denote by

$$K^{\star}(G) = \{ [g, \varphi] \mid g \in G, \varphi \in Aut(G) \}$$

the set of all autocommutators of G and, following [2], we write

$$G^{\star} = \langle K^{\star}(G) \rangle.$$

D. Garrison, L-C. Kappe and D. Yull proved in [1] that in a finite abelian group the set of autocommutators always forms a subgroup. Furthermore they found a nilpotent group of class 2 and of order 64 in which the set of all autocommutators does not form a subgroup, and they proved that it is an example of minimal order.

In this talk we will discuss the relationship between $K^{\star}(G)$ and G^{\star} in infinite abelian groups, as done in [3] jointly with L-C. Kappe and M. Maj.

References

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